# TB(2B) Ch. 11 Areas & Volumes (II) Conventional Questions

## 1. [13-14 Final Exam #11]

Four identical metal cylinders of base radii 2 cm and height h cm are melted and recast into a new cylinder of the same height.

(a) Find the volume of the new cylinder in terms of  $\pi$  and h.

(1 mark)

(b) Peter claims that the total surface area of the new cylinder is larger than that of the original four metal cylinders. Do you agree? Explain your answer. (3 marks)

# 2. [13-14 Final Exam #12]

In **Figure 4,** sector AOB with radius 1 cm and sector COD with radius 2 cm have a common centre O. AOD and OBC are straight lines. If the perimeter of sector AOB is equal to that of sector COD, find  $\theta$ .

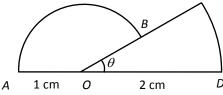


Figure 4

## 3. [13-14 Final Exam #13]

In **Figure 5(a)**, rectangle ABCD with dimensions  $a \text{ cm} \times b$  cm is inscribed in a circle with diameter d cm. In **Figure 5(b)**, four semi-circles are then constructed with their diameters to be each of the four sides of the rectangle. Show that the total area of the shaded regions is  $ab \text{ cm}^2$ .

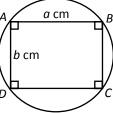


Figure 5(a)

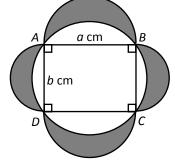


Figure 5(b)

#### 4. [14-15 Final Exam #14]

In **Figure 5**, the sector *OAD* is cut from the sector *OBC*. It is given that

 $\angle BOC = 120^{\circ}$ , OD = 2r cm, DC = r cm and the perimeter of shaded region ABCD is  $(6+10\pi)$  cm. Find the area of the shaded region ABCD. (3 marks)

(Give the answer in terms of  $\pi$ .)

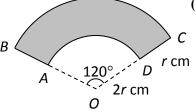


Figure 5

## 5. [15-16 Final Exam #8]

It is given that a cylindrical tank of base diameter 8 cm and height 20 cm contains some water.

(a) Find the curved surface area of the tank.

- (2 marks)
- (b) If the volume of water in the tank is  $240\pi$  cm<sup>3</sup>, find the height of the water level. (2 marks)
- (c) Write down the percentage increase of the capacity of the tank if the base diameter and the height are both increased by 10%. (1 mark)

## 6. [15-16 Final Exam #15]

**Figure 7** shows a metallic prism. It has a cross-section of a sector with radius r and height h. The angle subtended by the arc of the sector is  $60^{\circ}$ . There is a cylinder with same radius and of height k. It is given that the total surface areas of the prism and the cylinder are the same. Janice claims that k is less than half of h. Do you agree? Explain your answer. (3 marks)

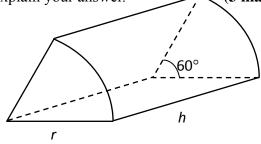


Figure 7

# 7. [16-17 Final Exam #12]

**Figure 4** shows a slice of a cake in shape of a prism with sector OAB as its uniform cross-section. It is known that the angle at centre O is  $45^{\circ}$  and the radius of the sector is 8 cm. If the volume of the cake is  $80\pi$  cm<sup>3</sup>,

(a) find the height of the cake.

- (2 marks)
- (b) The slice of the cake is then cut into two equal parts such that the angle at centre of each section becomes 22.5°. Find the total surface area of the two smaller slices of the cake, including their bases. (2 marks)

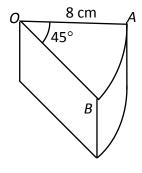


Figure 4