# St. Stephen's Girls' College <br> Final Examination 2017-2018 

## Form 2 <br> 170 students <br> MATHEMATICS <br> Paper II <br> Time Allowed: 1 hour

Name: $\qquad$ No.: $\qquad$ Class: $\qquad$ Division: $\qquad$

## Instructions:

- Answer ALL questions in the spaces provided in this Question-Answer Paper.
- All rough work should be done on the rough work paper provided, but will not be marked.
- The diagrams in this paper are not necessarily drawn to scale.
- Unless otherwise specified, numerical answer should be either exact or correct to 3 significant figures.
- This paper carries 100 marks.

1. Simplify $\left(\frac{a}{b}\right)^{3} \times a^{4}$.
2. Expand the following expressions.
(a) $b(2 b+1)$
(b) $(x+3)(4-2 x)$
3. If $x=6$ is a solution of $3(x-3)=4(x+k)-7$, find $k$.
4. Determine whether the following statements are true or false and circle the correct answers.
(a) $2 x^{2}-8=2(x-2)^{2}$
(b) $(9 a-b)(9 a+b)=18 a^{2}-b^{2}$
(c) $(-a+4)^{2}=(-4+a)^{2}$
5. If $(2 x+3)(x+a) \equiv 2 x^{2}+b(x+1)$, find the value of $a$.
6. The volume of a solid is measured as $200 \mathrm{~cm}^{3}$, correct to 2 significant figures. Find the upper limit of the actual volume of the solid.
7. The base and the height of a triangle are measured as 6.0 cm and 2.0 cm correct to the nearest 0.5 cm respectively. Let $x \mathrm{~cm}^{2}$ be the actual area of the triangle. Find the range of values of $x$.
8. Solve $\left\{\begin{array}{l}x-4 y=5 \\ x+4 y=9\end{array}\right.$.
9. Mark bought 2 bars of chocolate and 2 bottles of apple juice for $\$ 26$. Susan bought 1 bar of chocolate and 4 bottles of apple juice for $\$ 37$. How much is a bottle of apple juice?
10. $(2,3)$ is the solution of the simultaneous equations $\left\{\begin{array}{l}4 x+3 y=17 \\ x-y=-1\end{array}\right.$. Solve $\left\{\begin{array}{l}\frac{4}{x}+9 y=17 \\ \frac{1}{x}-3 y=-1\end{array}\right.$.

Answers

1. $\qquad$
2. 

(a) $\qquad$
(b) $\qquad$
3. $\qquad$
4.
(a) True / False
(b) True / False
(c) True / False
5. $\qquad$
6. $\qquad$
7. $\qquad$
8. $x=$ $\qquad$

$$
y=
$$

$\qquad$
9. $\qquad$
11. The following frequency distribution table shows the time taken (in min) by a group of students to finish their lunch.

| Time <br> $(\min )$ | $8-12$ | $13-17$ | $18-22$ | $23-27$ | $28-32$ |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Frequency | 6 | 12 | 18 | 10 | 4 |

(a) If the time taken by a student is 27.5 minutes, which class interval does it belong to?
(b) Find the class width of each class interval.
(c) Find the percentage of students who finish their lunch in less than 17.5 minutes.
12. The following histogram shows the weight distribution of a group of boys.

Weights of a group of boys

(a) How many boys are in the group?
(b) What is the lowest possible weight of the heaviest boy?
13. The following frequency curves show the distribution of the ages of members of the chess club and the bridge club in a community centre. Determine whether the members of the chess club or the bridge club are older on the whole.

14. A shop sells 518 pairs of shoes in 2 weeks. Express the rate of selling shoes in pairs/day.
11.
(a) $\qquad$
14. $\qquad$
(a)
(b) $\qquad$
13. $\qquad$
15. Jay's home is 1.8 km from his office. His average walking speed is $1.2 \mathrm{~m} / \mathrm{s}$. If he leaves home and walks to his office at 6:30 a.m., when will he arrive at his office?
16. If $6 x=7 y$, find $x: y$.
17. If $a: b=4: 9$ and $a: c=3: 7$, find $a: b: c$.
18. The prices of a book and a dictionary are in the ratio $4: 5$, and the price of the book is $\$ 50$ lower than that of the dictionary. Find the price of the book.
19. If the length of a highway on a map is 8 cm and its actual length is 12 km , express the scale of the map in the form $1: n$.
20. In the figure, $A C E F$ and $B D C$ are straight lines, $\triangle A B C$ is an equilateral triangle and $\angle C D E=22^{\circ}$. Find $\angle D E F$.

21. In $\triangle A B C, A B=A C$ and $\angle B=46^{\circ}$. Find $\angle A$.
22. Find the sum of interior angles of a 22 -sided polygon.
23. The size of each interior angle of a regular $n$-sided polygon is $150^{\circ}$. Find the value of $n$.
24. In the figure, $A B C D E$ is a part of a regular polygon. $A B$ produced and $E D$ produced intersect at $P$. If $\angle C=162^{\circ}$, find $\angle P$.

15. $\qquad$
20. $\qquad$
25. In the figure, find the value of $y$.

26. In the figure, $A B C D$ is a square. If the area of $A B C D$ is 32 , find the length of $B D$.

27. In $\triangle D E F, \angle E=90^{\circ}$ and $D E=20 \mathrm{~cm}$. If the area of $\triangle D E F$ is $210 \mathrm{~cm}^{2}$, find the perimeter of $\triangle D E F$.
28. In the figure, $P Q=x \mathrm{~cm}, Q R=8 \mathrm{~cm}$ and $R S=10 \mathrm{~cm}$. If the distance between $P$ and $S$ is $(x+12) \mathrm{cm}$, find the value of $x$.

29. Simplify the following expressions:
(a) $\sqrt{48}+\sqrt{12}$
(b) $\sqrt{3} \times \sqrt{18}$
30. In the figure, $M$ is the mid-point of $Q R$. If $P Q=5$ and $Q R=8$, find
(a) $\angle P M Q$,
(b) $\angle M P R$.

31. In the figure, find the area of the trapezium.
(Leave the radical sign " $\sqrt{ }$ " in the answer.)

32. In $\triangle A B C, \angle B=90^{\circ}, A C=5$ and $B C=4$.

Find $\angle A$ and $\angle C$.
33. In the figure,
$A B: C D=1: n$. Find the value of $n$.
(Leave the radical sign " $\sqrt{ }$ " in the answer.)

34. If $x$ is an acute angle such that $\cos x=\frac{4}{7}$, find the value of $\tan x$ in surd form. Simplify and rationalize the denominator of your answer if necessary.
35. Find the acute angle $x$ in each of the following.
(a) $\tan 2 x=\frac{1}{\tan 30^{\circ}}$
(b) $\cos 5 x=\sin 4 x$
32.
$\angle A=$
2
2

3
(b) $\qquad$

Subtotal:/ 15

