

**St. Stephen's Girls' College**  
**Final Examination 2016-2017**

**Form 2**  
**168 students**

**LC, WMC, LHK, LL, CYN, MLW**

**MATHEMATICS**  
**Paper II**  
**Time Allowed: 1 hour**

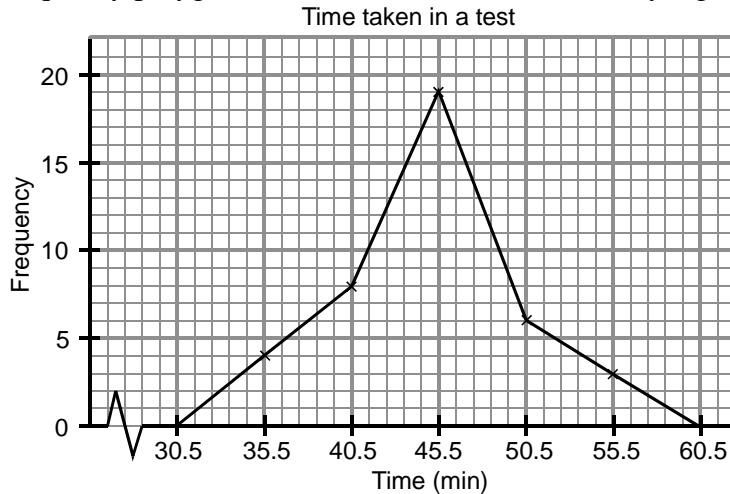
**Name:** \_\_\_\_\_ **No.:** \_\_\_\_\_ **Class:** \_\_\_\_\_ **Division:** \_\_\_\_\_

**Instructions:**

- Answer **ALL** questions in the spaces provided in this **Question-Answer Paper**.
- All rough work should be done on the rough work paper provided, but will not be marked.
- The diagrams in this paper are not necessarily drawn to scale.
- This paper carries 100 marks.

	<u>Answers</u>	<u>Marks</u>
1. Simplify $2^{2n} \times 8^{3n}$ .	1. _____	3
2. Expand $(x + 6)(x + 2)$ .	2. _____	2
3. Determine whether the following statements are true or false and circle the correct answers. (a) $x^2 - 4^2 = (x - 4)^2$ (b) $(3x + y)(3x - y) = 3x^2 - y^2$ (c) $(1 - b)^2 = (b - 1)^2$	3. (a) True / False (b) True / False (c) True / False	1 1 1
4. Make $q$ the subject of the formula $p = \frac{1}{3}qr^2$ .	4. _____	2
5. A bottle is termed <i>standard</i> if its capacity is measured as 200 mL, correct to the nearest 10 mL. Find the least capacity of a <i>standard</i> bottle.	5. _____	2
6. Stephen spent 12.06 s to complete a 100 m race, correct to 4 significant figures. Find the maximum error of the measured time.	6. _____	2
7. The length of a piece of metal wire is measured as 2.0 m, correct to the nearest 0.1 m. Peter cuts this metal wire into $n$ pieces of shorter wires, with each length measured as 5 cm correct to the nearest cm. Find the greatest possible value of $n$ .	7. _____	3
	Subtotal:	/17

8. The following frequency polygon shows the time taken in a test by a group of students.



(a) Find the class width of each class interval.

(b) For the class interval with the highest frequency, find

(i) its frequency,

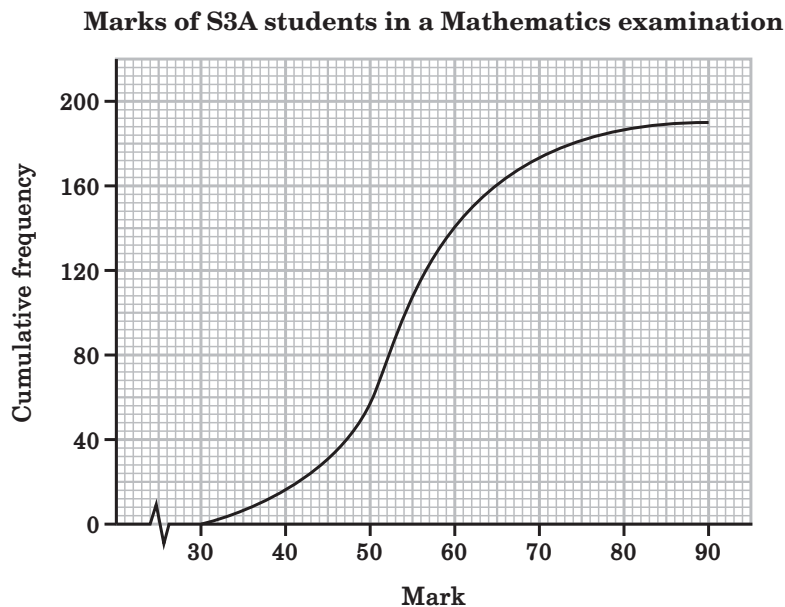
(ii) its class mark,

(iii) its class boundaries.

(c) What is the shortest possible time taken by the group of students?

8.		
(a)	_____	2
(b)		
(i)	_____	1
(ii)	_____	1
(iii)	_____	2
(c)	_____	2

9. The following cumulative frequency curve shows the marks of 190 S3A students of a school in a Mathematics examination.



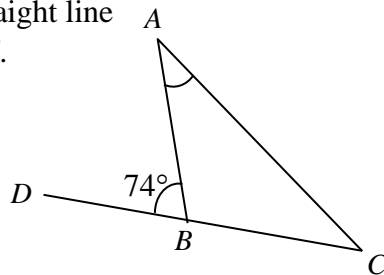
(a) How many students got 60 marks or more?

(b) If the passing mark is 40, find the passing percentage of the examination. (Correct the answer to 3 significant figures.)

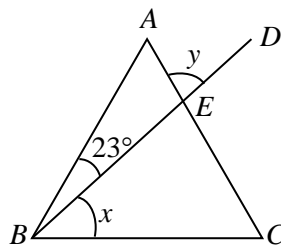
9.		
(a)	_____	1
(b)	_____	2

Subtotal: /11

10. Which of the following points lies on the graph of the equation  $y = 3x - 5$ ?  
 $A(-2, 1)$ ,  $B(-1, -2)$ ,  $C(-5, 0)$ ,  $D(3, 4)$
11. If the graph of the equation  $3x + y = 12$  passes through  $P(m + 8, m)$ , find the value of  $m$ .
12. Solve the simultaneous equations  $\begin{cases} 9u = 3v + 6 \\ 9u = 4 - v \end{cases}$ .
13. David has some \$10 and \$2 coins that worth \$90 in total. If there are a total of 13 coins, how many \$10 coins does David have?
14. Mary has 10 English books, 8 Chinese books and 2 Japanese books. Find the ratio of the number of English books to that of Chinese books to that of Japanese books.
15. If  $4x = 9y$ , find  $x : y$ .
16. If  $a : c = 3 : 10$  and  $b : c = 5 : 4$ , find  $a : b : c$ .
17. Twelve packs of green tea are sold for \$38.4. Find the price rate in \$/pack.
18. Susan buys the first 24 cans of cola at \$ $x$ /can and the next 8 cans of cola at \$ $(x + 0.4)$ /can. If the average cost of the cola is \$3.4/can, find the value of  $x$ .
19. In the figure,  $DBC$  is a straight line and  $AB = BC$ . Find  $\angle BAC$ .



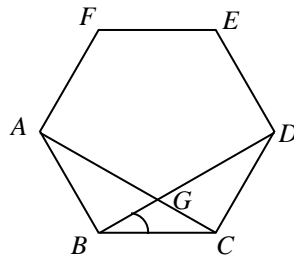
20. In the figure,  $\triangle ABC$  is an equilateral triangle.  $BD$  and  $AC$  intersect at  $E$ . Find  $x$  and  $y$ .



10. \_\_\_\_\_ 2
11. \_\_\_\_\_ 3
12.  $u =$  \_\_\_\_\_ 2  
 $v =$  \_\_\_\_\_ 2
13. \_\_\_\_\_ 3
14. \_\_\_\_\_ 2
15. \_\_\_\_\_ 2
16. \_\_\_\_\_ 3
17. \_\_\_\_\_ 2
18. \_\_\_\_\_ 3
19. \_\_\_\_\_ 2
20.  $x =$  \_\_\_\_\_ 1  
 $y =$  \_\_\_\_\_ 2

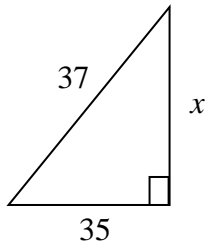
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21. In the figure,  $ABCDEF$  is a regular hexagon.  $AC$  and  $BD$  intersect at  $G$ . Find  $\angle DBC$ .

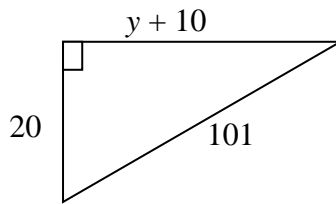


22. The size of each exterior angle of a regular  $n$ -sided polygon is  $18^\circ$ . Find the value of  $n$ .
23. Find the unknowns in the following figures.

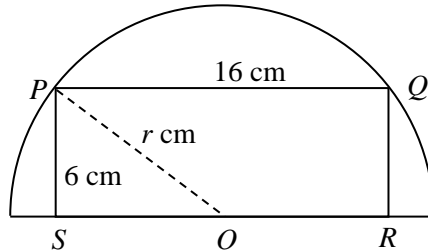
(a)



(b)



24. In the figure,  $PQRS$  is a rectangle with  $R$  and  $S$  lie on the diameter of a semicircle.  $PQ = 16$  cm,  $PS = 6$  cm and  $OP = r$  cm. If  $OP$  is the radius of the semicircle, find  $r$ .



25. In  $\triangle ABC$ ,  $AB = 7$ ,  $BC = \sqrt{18}$  and  $CA = \sqrt{31}$ . Determine whether  $\triangle ABC$  is a right-angled triangle. (Circle the correct answer.)

26. Which of the following is NOT a rational number?  
 $3.\dot{9}$ ,  $\frac{2}{7}$ ,  $\sqrt{25} + 1$ ,  $\sqrt{3}$

27. Simplify the following expressions.

(a)  $7\sqrt{3} + 2\sqrt{3} - 3\sqrt{3}$

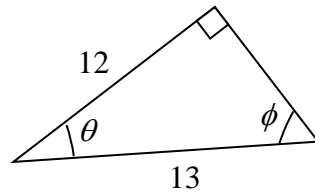
(b)  $\sqrt{72} - \sqrt{50}$

28. Simplify  $(\sqrt{x+1} + \sqrt{x})(\sqrt{x+1} - \sqrt{x})$ .

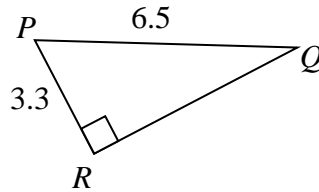
21.	_____	3
22.	_____	2
23.		
(a)	$x =$ _____	2
(b)	$y =$ _____	3
24.	_____	2
25.	Yes / No	2
26.	_____	1
27.		
(a)	_____	2
(b)	_____	2
28.	_____	2
Subtotal:		/21

29. In the following figure, find the value of each of the following and give the answers in fractions.

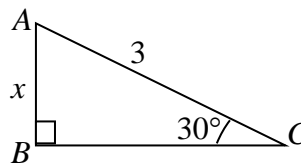
- (a)  $\cos \theta$
- (b)  $\sin \theta$
- (c)  $\tan \phi$



30. In the figure, find  $\angle P$ .  
Correct your answer to 3 significant figures.



31. In the figure,  $\angle ABC = 90^\circ$ ,  
 $\angle ACB = 30^\circ$  and  $AC = 3$ .  
Find  $x$ .



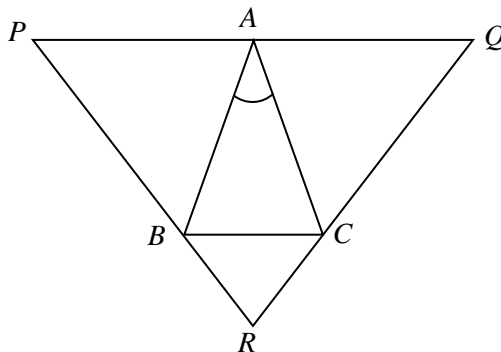
32. If  $x$  is an acute angle such that  $\sin x = \frac{7}{10}$ , find the value of  $\cos x$  in surd form. Simplify and rationalize the denominator of your answer if necessary.

33. Simplify  $9 - \sin^2 x - \cos^2 x$ .

34. Find the acute angle  $x$  such that  $\sin x = \cos 55^\circ$ .

35. Find the acute angle  $x$  such that  $\tan x = \frac{1}{\tan 2x}$ .

36. In the figure,  $PAQ$ ,  $PBR$  and  $QCR$  are straight lines. It is given that  $AP = AB = AC = AQ$ ,  $PR = QR$  and  $\angle BRC = 2\angle BAC$ . Find  $\angle BAC$ .



29. (a) \_\_\_\_\_ 1

(b) \_\_\_\_\_ 2

(c) \_\_\_\_\_ 2

30. \_\_\_\_\_ 2

31. \_\_\_\_\_ 2

32. \_\_\_\_\_ 3

33. \_\_\_\_\_ 2

34. \_\_\_\_\_ 2

35. \_\_\_\_\_ 3

36. \_\_\_\_\_ 3

Subtotal: /22

---End of Paper ---