St. Stephen's Girls' College Final Examination 2016-2017

VC, LHK, KAL, CYN

Form 1 174 students

MATHEMATICS Paper I Time Allowed: 1 hour 30 minutes

Name: ()	Question No.	Marks	Question No.	Marks
Class: Division:	1		9	
	2		10	
Instructions:	3		11	
• Attempt <i>ALL</i> questions.	4		12	
• Write your answers in the spaces provided in this <i>Question-Answer Paper</i> .	5		13	
 <i>ALL</i> working must be clearly shown. The diagrams in this paper are not papagasily. 	6		14	
drawn to scale.	7		15	
• This paper carries 100 marks.	8		Total	

1. It is given that
$$S = \frac{17a - 1}{a + 1}$$
. If $S = \frac{59}{4}$, find the value of *a*.

(3 marks)

2. Solve the equation $\frac{x-4}{5} - x = 1$.

3. There are 20 questions in a game. 5 marks will be given for a correct answer. Otherwise be deducted	se, 3 marks will
(a) Peter got x answers correct. Express the marks of Peter in terms of x.	(3 marks)
(b) Is it possible for a student to get 0 mark in the game? Explain your answer.	(4 marks)

4. The pie chart below shows the favourite sports of the students in S1A.



It is known that 8 students in S1A choose 'Swimming' as their favourite sport.

- (a) Find the total number of students in S1A.
 (b) If 30% of students in S1A choose 'Basketball' as their favourite sport, find

 (i) x,
 - (i) x, (2 marks)
 (ii) the number of students in S1A who choose 'Badminton' as their favourite sport. (3 marks)

(2 marks)

- 5. A(-5, -2), B(3, -1), C(6, 4) and D(0, 6) represent the vertices of a quadrilateral ABCD. Let O be the origin. (3 marks)
 - (a) Draw the quadrilateral *ABCD* in a rectangular coordinate plane.
 - (b) Find the area of *ABCD*.
 - (c) The coordinates of a point P are (5, 0).
 - (i) Mark *P* in the coordinate plane in (a).
 - (ii) Hence, determine whether O and P lie inside or outside ABCD.



(3 marks)

(1 mark)

(1 mark)

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_	
6 Consider two points $A(3, 5)$ and $B(3, -2)$ AB cuts the r-axis at C	
(3, 3) and $D(3, 2)$. The cuts the x-axis at C.	
(a) Write down the coordinates of C	(2 marks)
(a) whice down the coordinates of C.	(2 marks)

(b) K is a point on the x-axis such that the area of ΔKAB is 14 sq. units. Find the two possible coordinates of K. (4 marks)

7. The figure shows a container in the shape of a prism. The shaded area is the lid of the container. It is given that the total surface area (including the lid) of the container is 588 cm².



(4 marks) (3 marks)

- (a) Find the value of *x*.(b) Find the capacity of the container.
- (c) If the container contains 54% of its capacity of water, find the depth of water if the container is placed upright as shown. (3 marks)



- 8. In the figure, the shaded region is the base of a metal prism.
 - (a) Find the area of the shaded region. (3 marks)
 - (b) It is given that the height of the prism is 12 cm. If the prism is melted and recast into another prism with height 10 cm, find base area of the new prism.(2 marks)



9. The figure shows a rectangle *R*.

U	U		
(a) Draw the imag	ge K after R is translated 4 units to the	right.	(2 marks)
(b) Draw the image	ge K' after K is rotated clockwise abou	t point <i>P</i> through 270°.	(2 marks)
(c) Draw the imag	ge R' after R is rotated clockwise about	t point <i>P</i> through 270°.	(2 marks)
(d) If R' undergoe	es a transformation to K', describe the t	ransformation.	(2 marks)

R				
		P		
	R			

- 10. In the figure, point Q is the image of point P after P is rotated anticlockwise about the origin O through 270°.
 - (a) Write down the coordinates of *P*.

(1 mark)

(5 marks)

- (b) Q is translated 18 units upwards and then 2 units to the right to a point R.
 - (i) Find the coordinates of R.
 - (ii) If P undergoes a transformation to R, describe the transformation.
 - (iii) Do *P*, *O* and *R* lie on the same straight line?



- 11. In the figure, *EGHD*, *AGB*, *AHC* and *BCF* are straight lines. *ED* // *BF*.
 - (a) Express $\angle ABC$ in terms of f. (1 mark)
 - (b) Find f. (2 marks)
 - (c) Determine if AB is parallel to DC, and give reasons. (4 marks)



- 12. In the figure, U is a point on PQ and PQ // RS.
 (a) Express x in terms of a. (5 marks)
 - (a) Express x in terms of a. (5 marks) (b) If $a = 65^{\circ}$, find x. (2 marks)





- 14. In the figure, *PQ* // *RS* and $\angle SQP = \angle RPS$.
 - (a) Prove that $\Delta PQS \sim \Delta SPR$.
 - (b) Find the perimeter of the quadrilateral PQSR. (4 marks)

Q \geq 21 18 R 27 S

(3 marks)

P

15. The stem-and-leaf diagram below shows the ages of the employees of a company.

Lea	uf(uni	<u>ts)</u>				
а	8	8	9			
0	1	1	3	4	6	6
1	6	8	8	9		
1	4					
0	1					
	<u>Lea</u> a 0 1 1 0	Leaf(unities a 8 0 1 1 6 1 4 0 1	Leaf(units) a 8 8 0 1 1 1 6 8 1 4 1 0 1 1	Leaf(units) a 8 8 9 0 1 1 3 1 6 8 8 1 4	Leaf(units) a 8 8 9 0 1 1 3 4 1 6 8 8 9 1 4 - - - 0 1 - - - 0 1 - - -	Leaf(units) a 8 8 9 0 1 1 3 4 6 1 6 8 8 9 4 1 4 4 5 5 6 1 4 5 5 5 5 0 1 5 8 9 5 5

- (a) If the difference between the age of the oldest employee and the age of the youngest employee is less than 35, write down all the possible values of *a*. (2 marks)
- (b) Find the percentage of employees with ages 40 or above. (2 marks)
- (c) After 5 years, the two oldest employees will leave the company and the company will not recruit new employees. Will the percentage of employees with ages 40 or above be greater than the answer in (b)? Explain your answer.(3 marks)